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SCALE INVARIANT VOLKOV–AKULOV SUPERGRAVITY

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ABSTRACT

A scale invariant Goldstino theory coupled to supergravity is obtained as a standard supergravity dual of a rigidly scale-invariant higher-curvature supergravity with a nilpotent chiral scalar curvature. The bosonic part of this theory describes a massless scalaron and a massive axion in a de Sitter Universe.

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1 Introduction

Motivated by single-field inflationary scenarios [1], several sgoldstinoless [2–5] supergravity extensions of inflationary models were recently considered [6–11] (for a recent review see [12]). Interestingly enough, in [7, 11] many of these models were linked to pure higher-derivative supergravity with a nilpotency constraint on the scalar curvature chiral superfield \mathcal{R} . These include the Volkov–Akulov–Starobinsky model [7] and the pure Volkov–Akulov theory coupled to supergravity [7]. Recently, the full component form of the latter theory was presented in [13, 14]

Along these lines, various authors considered R^2 theories of gravity [15] and their supergravity embeddings [15, 16], which possess a rigid scale invariance and naturally accommodate a de Sitter Universe. It is the aim of this note to give the sgoldstinoless version of these theories, which naturally combines an enhanced rigid scale invariance and a de Sitter geometry. This theory also emerges as a limiting case of the inflationary scenario.

2 Scale-Invariant Nilpotent Supergravity

The superspace action density of the scale-invariant theory that we consider ³,

$$\mathcal{A} = \left. \frac{\mathcal{R} \overline{\mathcal{R}}}{g^2} \right|_D + \left. \sigma \mathcal{R}^2 S_0 \right|_F , \quad (2.1)$$

where g is a dimensionless parameter, is invariant under the rigid scale transformations

$$\mathcal{R} \rightarrow \mathcal{R} , \quad S_0 \rightarrow e^{-\lambda} S_0 , \quad \sigma \rightarrow e^\lambda \sigma . \quad (2.2)$$

This theory is equivalent to the theory considered in [16], supplemented with the nilpotency constraint

$$\mathcal{R}^2 = 0 , \quad (2.3)$$

which is enforced by the chiral Lagrange multiplier σ present in the second term of eq. (2.1).

Using manipulations similar to those originally introduced in [17], we can now turn this model into a scale-invariant version of the Volkov–Akulov model coupled to standard supergravity. To this end, we first use the superspace identity

$$\left. \sigma \mathcal{R}^2 S_0 + h.c. \right|_F = \left(\sigma \frac{\mathcal{R}}{S_0} + \bar{\sigma} \frac{\overline{\mathcal{R}}}{\overline{S}_0} \right) S_0 \overline{S}_0 \Big|_D + \text{tot. deriv.} , \quad (2.4)$$

³We use throughout the conventions of [7].

and then introduce two Lagrange chiral superfield multipliers T and S according to

$$\mathcal{A} = \left(\sigma S + \bar{\sigma} \bar{S} + \frac{S \bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D - T \left(\frac{\mathcal{R}}{S_0} - S \right) S_0^3 + \text{h.c.} \Big|_F . \quad (2.5)$$

The final result is the standard supergravity action density

$$\mathcal{A} = - \left(T + \bar{T} - \sigma S - \bar{\sigma} \bar{S} - \frac{S \bar{S}}{g^2} \right) S_0 \bar{S}_0 \Big|_D + T S S_0^3 + \text{h.c.} \Big|_F + \text{tot. deriv.} \quad (2.6)$$

A final shift and a redefinition according to

$$T \rightarrow T + \sigma S, \quad X = \frac{S}{g} \quad (2.7)$$

yield the standard supergravity action density

$$\mathcal{A} = - (T + \bar{T} - X \bar{X}) S_0 \bar{S}_0 \Big|_D + W(T, X) S_0^3 + \text{h.c.} \Big|_F , \quad (2.8)$$

where

$$W(T, X, \sigma) = g T X + g^2 \sigma X^2 . \quad (2.9)$$

This is tantamount to the scale-invariant superpotential

$$W(T, X) = g T X , \quad (2.10)$$

where X is subject to the nilpotency constraint

$$X^2 = 0 , \quad (2.11)$$

so that X describes the sgoldstinoless Volkov–Akulov multiplet [2–5]. The corresponding bosonic Lagrangian,

$$\mathcal{L} = \frac{R}{2} - \frac{3}{(T + \bar{T})^2} |\partial T|^2 - g^2 \frac{|T|^2}{3(T + \bar{T})^2} , \quad (2.12)$$

is a special case of the result displayed in [7], so that it describes an $SU(1, 1)/U(1)$ Kählerian model of curvature $-2/3$ with a scale-invariant positive potential. As a result, in terms of the canonical variable

$$T = e^{\phi \sqrt{\frac{2}{3}}} + i a \sqrt{\frac{2}{3}} , \quad (2.13)$$

one finds

$$\mathcal{L} = \frac{R}{2} - \frac{1}{2} (\partial\phi)^2 - \frac{1}{2} e^{-2\phi \sqrt{\frac{2}{3}}} (\partial a)^2 - \frac{g^2}{12} - \frac{g^2}{18} e^{-2\phi \sqrt{\frac{2}{3}}} a^2 . \quad (2.14)$$

Note that in the Einstein frame the metric is inert under the scale transformation corresponding to eq. (2.2), while

$$\phi \rightarrow \phi + \gamma , \quad a \rightarrow e^\gamma \sqrt{\frac{2}{3}} a . \quad (2.15)$$

3 de Sitter Vacuum Geometry

Since a is stabilized at zero, this model results in a de Sitter vacuum geometry, with a corresponding scale-invariant realization of supersymmetry breaking induced by the non-linear sgoldstinoless multiplet. The supersymmetry breaking scale M_s^2 is

$$M_s^2 = \frac{g}{2\sqrt{3}} M_{Planck}^2 , \quad (3.1)$$

up to a conventional numerical factor. Eq. (2.8) describes the minimal supergravity model that embodies a scale-invariant goldstino interaction and leads unavoidably to a de Sitter geometry. This model involves a single dimensionless parameter g , which determines its *positive* vacuum energy according to

$$V = \frac{g^2}{12} M_{Planck}^4 . \quad (3.2)$$

In contrast, the Volkov–Akulov model coupled to supergravity, depends on the two parameters f and W_0 , and consequently leads to a vacuum energy [18] [19] [20] [7] [13]

$$V = \frac{1}{3} |f|^2 - 3 |W_0|^2 \quad (3.3)$$

of arbitrary sign.

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